## TEMPERATURE DERIVATIVES OF VISCOSITY, DENSITY AND REFRACTIVE INDEX OF WATER-ETHANOL SYSTEM

## Part IV.—Measurements on the Activation Energy of Viscous Flow for Aqueous Ethanol Solutions from 11% to 24% at Intervals of 2.5% Ethanol

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The detailed study of the activation energy of viscous flow  $(E\eta = -T^2 \Delta \ln \eta / \Delta T)$  is now extended to concentrations from 11% to 24% ethanol. The measurements are made at intervals of 1°C on solutions whose concentrations differ by 2% to 3% ethanol. The temperature positions of the various jumps, classified as small, medium or large, can be readily connected by smooth curves, which link up with the earlier graphs for the range of 0% to 5% ethanol.

Some of the energy jumps are found to show subsidiary steps that grow in size as the concentration changes. Many such anomalous branchings are observed at concentrations lower than 6%, whereas the region from 11% to 16% shows a remarkable degree of stability. It appears probable that there are several significant structural changes corresponding to the branching out of these energy jumps, and finer studies in the range of 0% to 5% ethanol are in hand to elucidate this further.

### Introduction

In the previous communications on the activation energy of viscous flow, En, for aqueous ethanol solutions, I-3 it has been shown that  $E\eta$ exhibits stepwise variation for dilute alcohol and cyclic variation at the other end of the system. In a paper describing the measurements on  $E_{\eta}$ for 5% and 11% ethanol, the graphical comparison suggested a possible regular shift of corresponding energy jumps, with change in alcohol concentration.<sup>3</sup> In a later communication dealing with the finer study of these discontinuities in  $E_{\eta}$  from 0 to 30% ethanol, at the concentration intervals of 2%, it was noticed 4 that these shifts are functions of concentration, but are more or less abrupt in certain regions, e.g. between 26 to 42°C, especially for 2.5% to 6.9% ethanol solutions.

In an attempt to understand these puzzling phenomena, a study of temperature derivatives of the other physical properties, such as density and refractive index, has been undertaken and are being reported in the present series of papers. The detailed study on the accurate measurements of these derivative at close temperatures established a definite degree of correspondence between these phenomena, but revealed certain anomalies corresponding to some of the jumps observed in E/R.

In Part II of this series,<sup>5</sup> a detailed examination of the concentration dependence of energy jumps from 10°C to 50°C for dilute alcohol was undertaken, and it was noted that (cf. Fig. 3) the movement of these jumps with alcohol concentration are mostly smooth, but with some evidence of branching of these discontinuities into pairs concentrations, at certain accompanied by appearance and disappearance of certain steps. In order to throw further light, a series of experiments on 16.0%, 17.7%, 21.8% and 23.6% dilute ethanol solutions are reported in the present communication, and these, in combination with the published results 2,4,6 for 8.2%, 11%, 13.8% and 20% ethanol, give data at intervals of 2.5% concentration from 8% to 24% ethanol. An attempt is made to obtain a chart showing the broad variation for the temperature of each jump as a function of ethanol concentration on the pattern of that proposed for 0% to 5% alcohol in an earlier communication.

## **Experimental Procedure**

The measuring technique is the same as adopted in the previously reported experiments on the flow activation energy,  $E\eta$ , for water, aqueous alcohol <sup>2</sup>,4 and hydrocarbons. The values of E/R are calculated from the differential of the Andrade equation, *viz*. MEASUREMENT ON ACTIVATION ENERGY OF VISCOUS PLOW FOR AQUEOUS ETHANOL SOLUTIONS. PART IV 299.

$$\begin{split} & E\eta/R = \Delta \ln \eta/\Delta \left(\frac{1}{T}\right) = -T^2 \Delta \ln \eta/\Delta T \\ & = -T^2 \Delta \ln \nu/\Delta T + T^2 \beta \dots \dots (1) \\ & = E\nu/R + \beta T^2, \end{split}$$

where  $\nu$  kinematic viscosity  $= \eta/\rho$ , with  $\eta =$  dynamic viscosity and  $\rho =$  the density of substance.

Here  $\beta$  is the coefficient of dilatation, and T<sup>2</sup> $\beta$  forms a slowly varying correction term, which can be applied to the actual data for Ev/R. This basic differential technique has several advantages, such as the elimination of the constant of viscometer and the error in the calibration of stop watch, as well as an inherently high accuracy.

Five to six concordant readings for flow time in U-tube viscometer (No. '1', B.S.S. 188) are taken with a calibrated stop watch graduated to 0.1 sec., and read to an accuracy of  $\pm 0.02$  secs. The viscometer is supported in a Townson and Mercer thermostat having a thermistor bridge, giving temperature control to ±0.001°C or better, and the interval  $\Delta$  T, which is 1°C in all the subsequent experiments, is measured with the calibrated differential Beckmann thermometer graduated over a six-degree scale. Concentration of the solutions are checked at four to six stages during the whole course of the experiment, by density and viscosity determinations at appropriate temperatures. At higher temperatures, a ballast bottle containing the test liquid is connected to the viscometer and well immersed in the bath, to control the alcohol content by maintaining dynamic vapour-equilibrium.

# Experiments on 16.0% and 23.6% Dilute Ethanol

The first set of the measurements was carried out with 16% w/w aqueous ethanol solution in the range of  $10^{\circ}$  to  $50^{\circ}$ C, and the mean of E/R values for heating and cooling sequence is represented by the smooth curve drawn through solid circles of Fig. 1. Table 1(a) contains the overall mean E/R values together with their r.m.s. deviations for each set of five successive readings, estimated from those of the temperature and the time of flow; these deviations are of the order of  $\pm 0.005$ units of  $(E/R) \div 1000$ . For comparison with these measurements, the corresponding parts of the graphs for 13.8% and 11% ethanol are reproduced from the earlier work and shown (displaced downward by 0.05 and 0.10, respectively) as the full line and broken line curves of Fig. 1.

There is a general similarity of step-wise variation, with average step-length of  $3.8^{\circ}$ C and mean drop of the order of nearly 0.11 units of (E/R)/1000.

For further comparison with the reported data on 20% solution,4 the viscosity measurements on 23.6% ethanol were undertaken, again with the thermal interval of one degree C. Table 1(b) gives the mean temperatures, Beckmann readings, time of flow and calculated values of  $(E/R) \div 1000$ , together with their r.m.s. deviations (of the order of  $\pm 0.004$ ) obtained from groups of five successive readings covering the full Beckmann scale. The graph drawn through these (triangles) above the chain-line curve of the earlier data for 20% ethanol, represents the mean E/R values with an upward displaced scale. The succession of steps occurs at the average interval of 4.0°C with mean depth of 0.12 units (which is 30 time the r.m.s. experimental scatter), while the two largest jumps at 25°C. and 36°C. have depths of 0.15 and 0.18 units of  $(E/R) \div 1000$ .

## Results with 17.7% and 21.8% Ethanol and Discussion

In order to get a more clear picture of the movements of these discontinueties, it was considered worthwhile to complete the relatively large gaps left between 16.6% and 20% as well as 20% and 23.6% by extending the observations over two more solutions. Flow activation energy measurements are performed on 17.7% ethanol solution in the range of 10°C to 50°C, and the curve drawn through hollow circles, displaced 0.05 unit above 16.0% solution, in Fig. 1 represents the mean E/R values plotted against temperature, showing step-wise variation with the mean interval of  $4.3^{\circ}$ C and drop of 0.12 units of  $(E/R) \div 1000$ . The actual values for heating and cooling sequences, together with their r.m.s. scatter (which is of the order of 0.005 units of (E/R)/1000 are given in the Tables 2(a), and 2(b). Finally, a set of measurements was carried out on 21.8% ethanol solution, but the results are not plotted in Fig. 1, as those for 20% and 23.6% are too close together above 30°C.

The positions of the energy jumps, and their depths for all these seven concentrations covering the range from 11% to 24% ethanol are collected in Table 3. The temperature positions of the jumps as function of ethanol concentration are plotted in Fig. 2, the jumps being classified as large, medium or small, compared with the mean values of  $\frac{\Delta E/R}{1000/}$ =0.11±0.01. These are represented in Fig. 2 by circles, triangles and

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Fig. 1.—Plots of (E/R/1000, measured at intervals of one degree C for dilute ethanol solutions containing 11% to 24% e hanol. The vertical scale is correct for the middle graph for 16% ethanol, and successive graphs are shifted up or down by 0.05 unit of (E/R)/1000. Graphs without plotted points are based on published data.

crosses, respectively, while Fig. 3 is the corresponding chart for 0 to 5% ethanol based on the earlier data of Qureshi and Khan.<sup>5</sup>

It is seen that the various points plotted in Fig. 2 can be connected by smooth curves joining jumps that are of the same order of magnitude. While the region between 11% and 16% is remarkable for the near constancy in temperature of jumps, three branchings are observed in Fig. 2, which indicate the appearance or disappearance of a new jump. The graphs of Fig. 2 are further seen to join very satisfactorily onto those of Fig. 3, which are reproduced from the earlier experiments performed between 0% and 5% ethanol, using concentrations at the closer intervals of 1%. It is noteworthy that most of the anomalous branchings are to be found at concentrations lower than 6%ethanol. The additional data provided by the extension of the measurements to higher concentrations fills in certain details in the neighbourhood of 5% ethanol, and points out the probable directions for 3 or 4 branchings (shown by arrows) in the region of 3 to 7% ethanol. Further measurements are contemplated to finally decide the behaviour in the three regions marked X, Y and Z in Fig. 3.

Mean	E/R÷	$1000 = -T^2 \left( \Delta \ln \nu / \Delta T \right)$	/1000	Mean	$E/R \div 1$	$E/R \div 1000 = T^2 (\Delta \ln v / \Delta T) / 1000$				
rature °C.	Heating sequence	Cooling sequence	Overall mean	rature °C.	Heating sequence	Cooling sequence	Overall mean			
			and an and an and a second			namen Belandade Provinsion Belandade Provinsion	ganna hara- kara pana pana kara kara kara kara kara kara kara k			
10.50	$3.051 \pm 0.003$	$3.040 \pm 0.003$	$3.046 \pm 0.005$	31.50	$2.503 \pm 0.005$	$2.517 \pm 0.005$	$2.510 \pm 0.007$			
11.50	$3.066 \pm 0.003$	$3.084 \pm 0.003$	$3.075 \pm 0.009$	32.50	$2.497 \pm 0.005$	$2.505 \pm 0.005$	$2.501 \pm 0.004$			
12.50	$3.042 \pm 0.003$	$3.047 \pm 0.003$	$3.045 \pm 0.003$	33.50	$2.525 \pm 0.005$	$2.512 \pm 0.005$	$2.518 \pm 0.006$			
13.50	$2.952 \pm 0.003$	$2.938 \pm 0.003$	$2.945 \pm 0.007$	34.50	$2.385 \pm 0.005$	$2.392 \pm 0.005$	$2.389 \pm 0.003$			
14.50	$2.958 \pm 0.003$	$2.951 \pm 0.003$	$2.955 \pm 0.004$	35.50	$2.408 \pm 0.005$	$2.417 \pm 0.005$	$2.412 \pm 0.005$			
15.50	$2.954 \pm 0.004$	$2.967 \pm 0.004$	$2.961 \pm 0.006$	36.50	$2.387 \pm 0.005$	$2.379 \pm 0.005$	$2.383 \pm 0.004$			
16.50	$2.862 \pm 0.004$	$2.867 \pm 0.004$	$2.864 \pm 0.003$	37.50	$2.409 \pm 0.005$	$2.396 \pm 0.005$	$2.403 \pm 0.007$			
17.50	$2.876 \pm 0.004$	$2.865 \pm 0.004$	$2.870 \pm 0.005$	38.50	$2.287 \pm 0.005$	$2.294 \pm 0.005$	$2.291 \pm 0.003$			
18.50	$2.880 \pm 0.004$	$2.888 \pm 0.004$	$2.884 \pm 0.004$	39.50	$2.297 \pm 0.005$	$2.308 \pm 0.005$	$2.302 \pm 0.006$			
19.50	$2.811 \pm 0.004$	$2.794 \pm 0.004$	$2.803 \pm 0.009$	40,50	$2.296 \pm 0.004$	$2.290 \pm 0.004$	$2.293 \pm 0.003$			
20.50	$2.742 \pm 0.004$	$2.748 \pm 0.004$	$2.745 \pm 0.005$	41.50	$2.300 \pm 0.004$	$2.307 \pm 0.004$	$2.303 \pm 0.004$			
21.50	$2.771 \pm 0.004$	2.755±0.004	$2.763 \pm 0.008$	42.50	$2.236 \pm 0.004$	$2.225 \pm 0.004$	$2.231 \pm 0.004$			
22.50	$2.741 \pm 0.004$	$2.748 \pm 0.004$	2.745±0.004	43.50	$2.173 \pm 0.004$	<b>2.1</b> 68±0.004	$2.171 \pm 0.003$			
23.50	$2.749 \pm 0.004$	$2.742 \pm 0.004$	$2.746 \pm 0.004$	44.50	$2.162 \pm 0.004$	$2.171 \pm 0.004$	$2.167 \pm 0.004$			
24.50	$2.641 \pm 0.004$	$2.648 \pm 0.004$	$2.644 \pm 0.004$	45.50	$2.172 \pm 0.005$	2.178±0.005	$2.175 \pm 0.003$			
25.50	$2.662 \pm 0.005$	$2.673 \pm 0.005$	$2.667 \pm 0.006$	46.50	$2.157 \pm 0.005$	$2.152 \pm 0.005$	$2.155 \pm 0.003$			
26.50	$2.649 \pm 0.005$	$2.632 \pm 0.005$	$2.640 \pm 0.009$	47.50	$2.170 \pm 0.005$	$2.181 \pm 0.005$	$2.176 \pm 0.006$			
27.50	$2.652 \pm 0.005$	$2.662 \pm 0.005$	$2.657 \pm 0.005$	48.50	$2.154 \pm 0.004$	2.146±0.004	$2.150 \pm 0.004$			
28.50	$2.614 \pm 0.003$	$2.622 \pm 0.003$	$2.618 \pm 0.004$	49.50	$2.158 \pm 0.004$	<b>2.153</b> ±0.004	$2.156 \pm 0.003$			
29.50	$2.507 \pm 0.003$	$2.500 \pm 0.003$	$2.503 \pm 0.003$	50.50	2.159±0.004	2.163±0.004	$2.161 \pm 0.002$			
30.50	$2.501 \pm 0.003$	$2.496 \pm 0.003$	$2.498 \pm 0.003$							

# TABLE 1 (a).—MEASURED ACTIVATION ENERGIES $E/R \div 1000 = -T^2 (\Delta ln_v/\Delta T)/1000$ for 16.0%Aqueous Ethanol Solution in the Range of 10°C. To 50°C.

Heating sequence					Cooling sequence								
Tem- perature °C.	e Beckmann reading	Time of flow corrected for level	Mean tem- perature	uncorrect- ed	corrected	Tem- peratur °C.	e Beckmann reading	Time of flow corrected for level	Mean tem- perature	uncorrect- ed	corrected	Mean E/R÷1000	
1	2	3	4	5	6	7	8	9	10	11	12	23	
10.0	5.116±0.001	940.38±0.02	10.50	3.464	3.464+0.003	10.0	$5.113 \pm 0.000$	937.29±0.02	10.50	3.471	3.471±0.003	$3.468 \pm 0.004$	LAAA
11.0	4.114±0.001	$900.67 \pm 0.02$	11.50	3.468	3.487±0.003	11.0	$4.120 \pm 0.002$	897.98±0.01	11.50	3.483	3.484±0.003	$3.486 \pm 0.002$	BN
12.0	3.116±0.000	$862.81 \pm 0.01$	12.50	3.472	$3.472 \pm 0.003$	12.0	$3.120 \pm 0.000$	860.19±0.02	12.50	3.466	3.466±0.003	$3.469 \pm 0.003$	1. Q
13.0	$2.114 \pm 0.001$	$826.79 \pm 0.02$	13.50	3.468	$3.482 \pm 0.003$	13.0	$2.120 \pm 0.001$	$824.41 \pm 0.02$	13.50	3.482	3.478±0.003	$3.480 \pm 0.002$	URE
14.0	$1.116 \pm 0.000$	$792.51 \pm 0.01$	14.50	3.452	$3.452 \pm 0.003$	14.0	$1.124 \pm 0.000$	$790.33 \pm 0.01$	14.50	3.463	$3.463 \pm 0.003$	$3.458 \pm 0.006$	SHI,
15.0	$3.099 \pm 0.001$	$750.03\pm0.01$ $758.34\pm0.02$	15.50	3 391	$3396\pm0.003$	15.0	$3.070\pm0.000$	$759.75 \pm 0.01$ $759.75 \pm 0.01$	15 50	3,413	$3.411 \pm 0.003$	$3.404 \pm 0.007$	MA
16.0	$2.093 \pm 0.000$	$727.86 \pm 0.01$	16.50	3.322	3.420+0.003	16.0	$2.115 \pm 0.002$	$730.62 \pm 0.03$	16.50	3.311	$3.308 \pm 0.003$	3.314+0.006	õsoc
17.0	$1.111 \pm 0.001$	$700.10 \pm 0.02$	17.50	3,315	$3.314 \pm 0.003$	17.0	$1.094 \pm 0.000$	$701.74 \pm 0.01$	17.50	3.322	$3.321 \pm 0.003$	$3.317 \pm 0.004$	DDUE
$18.0 \\ 18.0$	$0.137 \pm 0.000$ $4.887 \pm 0.001$	$673.84 \pm 0.02$ $669.62 \pm 0.02$				18.0 18.0	$0.119 \pm 0.001$ $4.893 \pm 0.000$	$673.35 \pm 0.02$ $669.17 \pm 0.01$					RE
19.0	$3.813 \pm 0.000$	$642.54 {\pm} 0.01$	18.50	3.270	3.270±0.003	19.0	$3.843 \pm 0.001$	642.77±0.02	18.50	3.260	$3.260 \pm 0.003$	$3.265 \pm 0.005$	EHM
20.0	$2.814 \pm 0.000$	618.70±0.02	19.50	3.243	3.343±0.003	20.0	$2.856 \pm 0.000$	$619.22 \pm 0.01$	19.50	3.238	$3.239 \pm 0.003$	$3.241 \pm 0.002$	AN A
21.0	$1.810 \pm 0.000$	$595.70 \pm 0.01$ 595.39 + 0.02	20.50	5.255	$3.232 \pm 0.003$	21.0	$1.819 \pm 0.001$ 5.043 ± 0.000	$595.36 \pm 0.02$ $595.43 \pm 0.01$	20.30	5.207	$5.200 \pm 0.003$	J.239±0.007	ND ]
22.0	$4.000\pm0.000$	$573.30\pm0.02$	21.50	3.119	3.117±0.003	22.0	3.985+0.001	573.28+0.02	21.50	3.111	$3.110 \pm 0.003$	3.114±0.004	M. 1
23.0	3.005+0.001	$553.26 \pm 0.02$	21.50	3.125	$3.123 \pm 0.003$	23.0	$2.992 \pm 0.000$	$552.27 \pm 0.01$	22.50	3.126	$3.125 \pm 0.003$	3.124±0.001	M. (
23.0	$4.360 \pm 0.000$	$554.25\pm0.02$	23.50	3.095	$3.091 \pm 0.004$	23.0	4.360±0.001	554.27±0.02	23.50	3.119	$3.114 \pm 0.004$	3.102±0.001	QUR
24.0	$3.320 \pm 0.001$	$534.31 \pm 0.03$	24.50	3.129	$3.127 \pm 0.004$	24.0	$3.321 \pm 0.000$	$534.23 \pm 0.02$	24.50	3.113	$3.112 \pm 0.004$	$3.120 \pm 0.007$	ASHI
25.0	$2.297 \pm 0.000$	$515.35 \pm 0.02$	25.50	2.978	$2.978 \pm 0.004$	25.0	$2.398 \pm 0.001$	$516.18 \pm 0.03$	25.50	2.958	$2.958 \pm 0.004$	$2.968 \pm 0.010$	
26.0 26.0	$1.305 \pm 0.001$ $4.166 \pm 0.000$	$498.59 \pm 0.02$ $501.30 \pm 0.01$	26 50	2 067	$2.967 \pm 0.003$	26.0	$1.362 \pm 0.000$ $4.168 \pm 0.000$	$501.24 \pm 0.02$	26.50	2 981	2 981 - 0 003	2 974-10 007	
27.0	$3.170 \pm 0.001$	485.07±0.02	27.50	2.971	$2.970 \pm 0.003$	27.0	$3.196 \pm 0.001$	$485.32 \pm 0.01$	27.50	2.980	$2.980 \pm 0.003$	$2.975 \pm 0.005$	
28.0	$2.125 \pm 0.000$	468.66±0.01	28.50	2,951	2.952+0.003	28.0	$2.116 \pm 0.000$	468.36±0.02	28,50	2.965	2.966±0.003	2.959±0.007	
29.0	$1.095 \pm 0.000$	453.26±0.02	29.50	2.976	$2.976 \pm 0.003$	29.0	1.126±0.000	453.49±0.01	29.50	2.965 2	$2.965 \pm 0.003$	2.970⊣0.005	
30.0	$0.058 \pm 0.001$	438.21±0.02				30.0	$0.069 \pm 0.001$	$438.24 \pm 0.02$				(Continued)	

Table 1 (b).—Beckmann Readings, Flow Times (Seconds) and Calculated Values of  $E/R \div 1000 = -T^2 (\Delta \ln \nu/\Delta T) / 1000$  for 23.7% Aqueous Ethanol from 10°C. to 54°C.

(TABLE I ()	c) Continued)
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1	2	3	4	5	6	7	8	9	10	11	12	13	ASU
30.0	4.044±0.000	$438.80 \pm 0.02$	20 50	0.012	0.01(1.0.001	30.0	4.043±0.001	438.79±0.01	20 50	0.025	0.027.1.0.004	0.040 + 0.005	REN
31.0	$2.998 \pm 0.001$	424.26±0.02	30.50	2,943	$2.946 \pm 0.004$	31.0	$3.020 \pm 0.001$	424.73±0.02	30.50	2.935	$2.937 \pm 0.004$	$2.942 \pm 0.005$	IEN
32.0	$1.965 \pm 0.000$	$410.72 \pm 0.01$	31.50	2.941	$2.942 \pm 0.004$	32.0	$2.021 \pm 0.000$	$410.49 \pm 0.02$	31.50	2.942	$2.942 \pm 0.004$	$2.942 \pm 0.001$	TS (
33 0	0.963-0.001	398 39 - 0 02	32.50	2.844	$2.843 \pm 0.004$	33 0	0.965+0.001	398 53 + 0.01	32.50	2.831	$2.831 \pm 0.004$	$2.837 \pm 0.006$	N NC
24.0	0.000 _ 0.001	396.09 + 0.02	33.50	2.867	$2.863 \pm 0.004$	24.0	0.903±0.001	306.13±0.01	33.50	2.846	$2.841 \pm 0.004$	$2.852 \pm 0.011$	ACT
34.0	$2.154 \pm 0.001$	$386.29 \pm 0.02$	34.50	2,835	$2.834 \pm 0.004$	34.0	$2.192 \pm 0.000$	$386.12\pm0.02$	34.50	2.841	$2.840 \pm 0.004$	$2.837 \pm 0.003$	IVA
35.0	$1.154 \pm 0.000$	$374.89 \pm 0.01$	35 50	2.847	$2.847 \pm 0.004$	35.0	$1.191 \pm 0.001$	$374.69 \pm 0.01$	35.50	2.841	$2.840 \pm 0.004$	$2.844 \pm 0.004$	TIO
36.0	$0.173 \pm 0.001$ $4.500 \pm 0.000$	$364.06 \pm 0.02$ $363.65 \pm 0.01$				36.0 36.0	$0.203 \pm 0.001$ $4.517 \pm 0.000$	$363.81 \pm 0.02$ $363.52 \pm 0.02$					z
37 0	3 483+0 001	353 54 + 0.02	36.50	2.666	$2.666 \pm 0.004$	37.0	3 494 + 0 001	353 44 1 0 02	36.90	2.635	$2.635 \pm 0.004$	$2.650 \pm 0.015$	NEI
20.0	0.475 L 0.000	333.34±0.02	37.50	2.662	$2.667 \pm 0.004$	20.0	5.494±0.001	333.44±0.02	37.50	2.663	$2.668 \pm 0.004$	$2.668 \pm 0.001$	RGY
38.0	2.475±0.000	$343.84\pm0.01$	38.50	2.656	$2.654 \pm 0.004$	38.0	$2.483 \pm 0.000$	$343.69\pm0.01$	38.50	2.639	$2.637 \pm 0.004$	$2.646 \pm 0.009$	OF
39.0	$1.465 \pm 0.001$	$334.47 \pm 0.01$	39.50	2,601	$2.605 \pm 0.004$	39.0	$1.493 \pm 0.001$	$334.57 \pm 0.02$	39.50	2.592	$2.596 \pm 0.004$	$2.600 \pm 0.004$	VI
40 0 40 0	$0.463 \pm 0.002$ 5.092+0.002	$325.67 \pm 0.03$ $324.57 \pm 0.03$				40.0	$0.460 \pm 0.000$ 5.075 $\pm 0.001$	$325.53 \pm 0.01$ $324.71 \pm 0.02$					SCOL
41 0	4 065 1 0 000	316 01 + 0.02	40.50	2.569	$2.560 \pm 0.005$	11 0	4.0551.0.000	316 34 10 01	40.50	2.543	$2.544 \pm 0.005$	$2.552 \pm 0.008$	us I
42.0	4.003±0.000	$310.01 \pm 0.02$	41.50	2.561	$2.560 \pm 0.005$	41.0	$4.035 \pm 0.000$	310.34±0.01	41.50	2.561	$2.560 \pm 0.005$	$2.560 \pm 0.009$	LO
42.0	3.089±0.001	$308.13 \pm 0.02$	42.50	2.566	$2.562 \pm 0.005$	42.0	$3.0/1\pm0.001$	$308.31 \pm 0.02$	42.50	2.565	$2.561 {\pm} 0.005$	$2.561 \pm 0.001$	WF
43.0	$2.082 \pm 0.000$	$300.24 \pm 0.01$	43.50	2.482	$2.482 \pm 0.005$	43.0	$2.081 \pm 0.000$	$300.55 \pm 0.02$	43.50	2.480	$2.480 \pm 0.005$	$2.481 \pm 0.001$	OR
44.0	$1.065 \pm 0.001$ $5.453 \pm 0.000$	$292.78 \pm 0.02$ $291.57 \pm 0.02$				44.0 44.0	$1.065 \pm 0.001$ $5.465 \pm 0.000$	$293.09 \pm 0.02$ $291.45 \pm 0.00$					AQ
45.0	4 451 + 0 001	284 45 + 0.01	44.50	2.488	$2.488 \pm 0.005$	45.0	4 518+0.001	284 69 1 0 02	44.50	2.482	$2.482 \pm 0.005$	$2.485 \pm 0.003$	UEO
16.0	2 475 + 0 000	207.79 0.01	45.50	2.491	$2.492 \pm 0.005$	45.0	4.510±0.001	207.02±0.02	45.50	2.497	$2.499 \pm 0.005$	$2.496 \pm 0.003$	US ]
40.0	3.4/3±0.000	277.72±0.02	46.50	2.479	$2.479 \pm 0.005$	40.0	3.519±0.000	277.78±0.02	46.50	2.482	$2.482 \pm 0.005$	$2.481 \pm 0.001$	Етн
47.0	$2.501 \pm 0.001$ $4.894 \pm 0.001$	$271.24 \pm 0.02$ $270.28 \pm 0.02$				47.0	$2.531 \pm 0.001$ $4.871 \pm 0.001$	$271.20\pm0.03$ $269.93\pm0.02$					ANG
48.0	3.871±0.000	263.66±0.01	47.50	2.492	$2.492 \pm 0.006$	48.0	3.878±0.000	263.56±0.01	47.50	2.474	$2.474 \pm 0.006$	$2.483 \pm 0.009$	E S
49.0	2.872 + 0.001	257.41 + 0.02	48.50	2.484	$2.482 \pm 0.006$	49.0	$2.890 \pm 0.001$	$257.38 \pm 0.02$	48.50	2.484	$2.481 \pm 0.006$	$2.482 \pm 0.001$	OLU
50.0	1 893+0 000	251 49+0 02	49.50	2.474	$2.470 \pm 0.006$	50.0	$1.892 \pm 0.000$	251 32+0 01	49.50	2.485	$2.481 \pm 0.006$	$2.475 \pm 0.006$	JTIC
50.0	$5.028 \pm 0.001$	$251.71 \pm 0.02$	50 50	2 360	2 370 1 0 006	50.0	$5.033 \pm 0.000$	$251.70\pm0.01$	50.50	2.300	2 200 1 0 006	2 379 1 0 001	ONS.
51.0	$4.026 \pm 0.001$	246.08±0.02	50.50	0.204	2.370±0.000	51.0	4.045±0.001	246.09±0.02	50.50	2.370	2.300±0.000	2.375±0.001	PA:
52.0	3.029±0.000	$240.60 \pm 0.01$	51.50	2.381	2.382±0.006	52.0	$3.035 \pm 0.000$	$240.53 \pm 0.02$	51.50	2.386	2.48/±0.006	$2.385 \pm 0.003$	RT
53.0	$2.021 \pm 0.001$	$235.22 \pm 0.02$	52,50	2.379	$2.380 \pm 0.006$	53.0	$2.035 \pm 0.001$	$235.21 \pm 0.02$	52.50	2.368	$2.369 \pm 0.006$	$2.375 \pm 0.006$	VI
54.0	$1.029 \pm 0.000$	230.09±0.01	53.50	2.372	$2.373 \pm 0.006$	54.0	$1.034 \pm 0.001$	230.02+0.02	53.50	2.379	$2.380 \pm 0.006$	$2.376 \pm 0.004$	30
										×	1		\$

MEAS

## TAYEB M. QURESHI, MAQSOODUR REHMAN AND M. M. QURASHI

*Tempera- ture °C,		E/R÷	$1000 = T^2 (\Delta \ln v)$	/ΔT) 1000	Tempe-	$E/R \div 1000 = -T^2 (\Delta \ln_\nu / \Delta T)) 1000$				
		Heating sequence	Cooling sequence	Overall mean	°C.	Heating sequence	Cooling sequence	Overall mean		
	9.50	$3.276 \pm 0.003$	$3.285 \pm 0.003$	3,280+0.005	31.50	$2.730 \pm 0.004$	2.721 + 0.004	$2.725 \pm 0.005$		
	10.50	$3.301 \pm 0.003$	$3.289 \pm 0.003$	$3.295 \pm 0.006$	32.50	$2.594 \pm 0.004$	$2.606 \pm 0.004$	$2.600 \pm 0.006$		
	11.50	$3.157 \pm 0.003$	$3.164 \pm 0.003$	$3.161 \pm 0.003$	33.50	$2.613 \pm 0.004$	$2.608 \pm 0.004$	$2.610 \pm 0.003$		
	12.50	$3.179 \pm 0.003$	$3.171 \pm 0.003$	$3.175 \pm 0.004$	34.50	$2.601 \pm 0.004$	$2.610 \pm 0.004$	$2.605 \pm 0.004$		
	13.50	$3.153 \pm 0.003$	$3.158 \pm 0.003$	$3.156 \pm 0.002$	35.50	$2.491 \pm 0.004$	$2.500 \pm 0.004$	$2.496 \pm 0.004$		
	14.50	$3.177 \pm 0.003$	$3.166 \pm 0.003$	$3.171 \pm 0.005$	36.50	$2.517 \pm 0.005$	$2.510 \pm 0.005$	$2.514 \pm 0.004$		
	15.50	$3.151 \pm 0.004$	$3.160 \pm 0.004$	$3.156 \pm 0.004$	37.50	$2.501 \pm 0.005$	$2.495\pm0.005$	$2.498 \pm 0.003$		
	16.50	$3.083 \pm 0.004$	$2.072 \pm 0.004$	$3.077 \pm 0.005$	38.50	$2.508 \pm 0.005$	$2.525 \pm 0.005$	$2.516 \pm 0.008$		
	17.50	$2.983 \pm 0.004$	$2.997 \pm 0.004$	$2.990 \pm 0.007$	39.50	$2.453 \pm 0.005$	$2.443 \pm 0.005$	$2.448 \pm 0.005$		
	18.50	$3.018 \pm 0.004$	$3.010 \pm 0.004$	$3.014 \pm 0.004$	40.50	$2.461 \pm 0.005$	$2.450 \pm 0.005$	$2.455 \pm 0.006$		
	19.50	$2.993 \pm 0.004$	$2.998 \pm 0.004$	$2.996 \pm 0.002$	41.50	$2.450 \pm 0.004$	$2.456 \pm 0.004$	$2.453 \pm 0.003$		
	20.50	$2.999 \pm 0.005$	$2.990 \pm 0.005$	$2.995 \pm 0.005$	42.50	$2.452 \pm 0.004$	$2.447 \pm 0.004$	$2.450 \pm 0.003$		
	21.50	$2.841 \pm 0.005$	$2.833 \pm 0.005$	$2.837 \pm 0.005$	43.50	$2.274 \pm 0.004$	$2.285 \pm 0.004$	$2.280 \pm 0.005$		
	22.50	$2.840 \pm 0.005$	$2.855 \pm 0.005$	$2.848 \pm 0.008$	44.50	$2.293 \pm 0.004$	$2.306 \pm 0.004$	$2.299 \pm 0.007$		
	23.50	$2.827 \pm 0.006$	$2.834 \pm 0.005$	$2.831 \pm 0.004$	45.50	$2.281 \pm 0.004$	$2.273 \pm 0.004$	$2.277 \pm 0.004$		
	24.50	$2.850 \pm 0.004$	$2.844 \pm 0.004$	$2.847 \pm 0.003$	46.50	$2.272 \pm 0.005$	$2.285 \pm 0.005$	$2.278 \pm 0.007$		
	25.50	$2.818 \pm 0.004$	$2.825 \pm 0.004$	$2.822 \pm 0.004$	47.50	$2.302 \pm 0.005$	$2.298 \pm 0.005$	$2.300 \pm 0.002$		
	26.50	$2.729 \pm 0.004$	$2.721 \pm 0.004$	$2.725 \pm 0.004$	48.50	$2.196 \pm 0.005$	$2.185 \pm 0.005$	$2.191 \pm 0.006$		
	27.50	$2.733 \pm 0.004$	$2.728 \pm 0.004$	$2.731 \pm 0.003$	49.50	$2.178 \pm 0.006$	$2.186 \pm 0.005$	$2.182 \pm 0.004$		
	28.50	$2.714 \pm 0.004$	$2.721 \pm 0.004$	$2.718 \pm 0.004$	50.50	$2.189 \pm 0.006$	$2.176 \pm 0.006$	$2.183 \pm 0.007$		
	29.50	$2.723 \pm 0.004$	$2.729 \pm 0.004$	$2.726 \pm 0.003$	51.50	$2.195 \pm 0.006$	$2.186 \pm 0.006$	$-2.190 \pm 0.005$		
	30.50	$2.725\pm0.004$	$2.710 \pm 0.004$	$2.718 \pm 0.008$						

## Table 2 (a).—Measured Activation Energies $E/R \div 1000 = -T^2(\Delta \ln \nu/\Delta T)/1000$ for 17.7% Aqueous Ethanol Solution in the Range of 9°C to 52°C.

Table 2 (b).—Measured Activation Energies E R : 1000—- $T^2(\Delta ln\nu/\Delta T)/1000$  for 21.8% Aqueous Ethanol in the Range of 10°C to 54°C at the Interval of 1°C.

Tempera-	E/R÷100	$00 = -T^2 (\Delta \ln \nu / \Delta $	т) 1000	Tempera-	$E/R \div 1000 = -T^2 (\Delta \ln \nu / \Delta T) 1000$				
ture °C.	Heating sequence	Cooling sequence	Overall mean	°C.	Heating sequence	Cooling sequence	Overall mean		
10.50	3.407+0.003	$3.420 \pm 0.003$	3.414±0.006	32.50	$2.820 \pm 0.004$	$2.829 \pm 0.004$	2.824±0.004		
11.50	$3.409 \pm 0.003$	$3.402 \pm 0.003$	$3.405 \pm 0.003$	33.50	$2.831 \pm 0.004$	$2.824 \pm 0.004$	$2.827 \pm 0.004$		
12.50	$3.424 \pm 0.003$	$3.417 \pm 0.003$	$3.421 \pm 0.004$	34.50	$2.812 \pm 0.004$	$2.829 \pm 0.004$	$2.821 \pm 0.009$		
13.50	$3.351 \pm 0.003$	$3.364 \pm 0.003$	$3.357 \pm 0.005$	35.50	$2.600 \pm 0.003$	$2.669 \pm 0.003$	$2.675 \pm 0.007$		
14.50	$3.358 \pm 0.003$	$3.351 \pm 0.003$	$3.354 \pm 0.004$	36.50	$2.676 \pm 0.003$	$2.682 \pm 0.003$	$2.679 \pm 0.003$		
15.50	$3.270 \pm 0.003$	3.279 + 0.003	3.275 + 0.004	37.50	$2.660 \pm 0.003$	$2.852 \pm 0.083$	$2.656 \pm 0.004$		
16.50	$3.297 \pm 0.003$	$3.291 \pm 0.003$	$3.294 \pm 0.003$	38.50	$2.692 \pm 0.003$	$2.681 \pm 0.003$	$2.687 \pm 0.005$		
17.50	$3.218 \pm 0.003$	$3.207 \pm 0.003$	$3.212 \pm 0.006$	39.50	$2.563\pm0.003$	$2.548 \pm 0.003$	$2.555 \pm 0.008$		
18.50	$3.200 \pm 0.003$	$3.205 \pm 0.003$	$3.203 \pm 0.003$	40.50	$2.578 \pm 0.005$	$2.573 \pm 0.005$	$2.575 \pm 0.003$		
19.50	$3.219 \pm 0.003$	$3.232 \pm 0.003$	$3.225 \pm 0.007$	41.50	$2.557 \pm 0.005$	$2.550 \pm 0.005$	$2.554 \pm 0.004$		
20.50	$3.158 \pm 0.004$	$3.165 \pm 0.004$	$3.162 \pm 0.004$	42.50	$2.552 \pm 0.005$	$2.563 \pm 0.005$	$2.558 \pm 0.005$		
21.50	$3.110 \pm 0.004$	$3.099 \pm 0.004$	$3.105 \pm 0.005$	43.50	$2.509 \pm 0.005$	$2.502 \pm 0.005$	$2.505 \pm 0.003$		
22.50	$3.123 \pm 0.004$	$3.130 \pm 0.004$	$3.126 \pm 0.003$	44.50	$2.476 \pm 0.005$	$2.463 \pm 0.005$	$2.470 \pm 0.007$		
23.50	$3.098 \pm 0.004$	$3.109\pm0.004$	$3.103 \pm 0.006$	45.50	$2.466 \pm 0.005$	$2.462 \pm 0.005$	$2.464 \pm 0.002$		
24.50	$3.029 \pm 0.004$	$3.017 \pm 0.004$	$3.0.23 \pm 0.006$	46.50	$2.501 \pm 0.005$	$2.489 \pm 0.005$	$2.495 \pm 0.006$		
25.50	$3.031 \pm 0.004$	$3.020 \pm 0.004$	$3\ 025 \pm 0.006$	47.50	$2.458 \pm 0.005$	$2.465 \pm 0.005$	$2.462 \pm 0.003$		
26.50	$2.972 \pm 0.004$	$2.977 \pm 0.004$	$2.975 \pm 0.003$	48.50	$2.483 \pm 0.005$	$2.476 \pm 0.005$	$2.480 \pm 0.004$		
27.50	$2.928 \pm 0.004$	$2.923 \pm 0.004$	$2.925 \pm 0.003$	49.50	$2.431 \pm 0.005$	$2.442 \pm 0.005$	$2.436 \pm 0.006$		
28.50	$2.915 \pm 0.004$	$2.922 \pm 0.004$	$2.918 \pm 0.004$	50.50	$2.384 \pm 0.005$	$2.376 \pm 0.005$	$2.380 \pm 0.004$		
29.50	$2.939 \pm 0.004$	$2.929 \pm 0.004$	$2.934 \pm 0.005$	51.50	$2.599 \pm 0.005$	$2.586 \pm 0.005$	2.4930.007		
30.50	$2.925 \pm 0.004$	$2.934 \pm 0.005$	$2.929 \pm 0.004$	52,50	$2.493 \pm 0.005$	$2.496 \pm 0.005$	$2.495 \pm 0.003$		
31.50	$2.907 \pm 0.004$	$2.904 \pm 0.004$	$2.905 \pm 0.002$	53.50	$2.482\pm0.005$	$2.475 \pm 0.005$	$2.476 \pm 0.000$		

Measurements on Activation Energy of Viscous Flow for Aqueous Ethanol Solutions. Part  $\mathrm{IV}_{305}$ 

Table 3.—Synopsis of the Observed Temperatures (in °C.) at the Jumps of (E/R)/1000, Together with the Magnitudes of these Jumps for Various Aqueous Ethanol. Solutions from 11.0% to 23.6% Ethanol.

11.0%	5	1.	Temperature at jump	13.8	-	19.2	23.3	27.1	32.0	35.1	40.8	46.0
ethanol	ì	2.	Depth of jump	0.16		0.10	0.11	0.11	0.10	0.07	0.12	0.06
13.8%	5	1.	Temperature at jump	13.2	15.1	19.2	23.1	28.1	33.1	37.1	40.9	46.0
ethanol	ĺ	2.	Depth of jump	0.11	0.08	0.10	0.12	0.11	0.12	0.07	0.11	0.07
16.0%	16.0%	1.	Temperature at jump	13.0	16.1	19.6	24.0	28.9	33.8	37.9	42.4	47.3
ethanol	1	2.	Depth of jump	0.10	0.08	0.12	0.10	0.14	0.11	0.10	0.13	0.07
17.7%	17.7%	1.	Temperature at jump	11.1	16.4	21.0	25.9	32.0	34.8	39.2	43.0	48.5
ethanol	i	2.	Depth of jump	0.12	0.16	0.16	0.11	0.12	0.09	0.10	0.11	0.10
20.0%	5	1.	Temperature at jump	13.6	16.9	20.8	24.2	30.0	34.8	39.0	42.6	49.9
ethanol	1	2.	Depth of jump	0.14	0.11	0.10	0.13	0.11	0.15	0.10	0.10	0.10
21.8%	5	1.	Temperature at jump	14.1	17.2	20.7	25.271.4	31.7	35.1	39.0	43.2	49.9
ethanol	1	2.	Depth of jump	0.13	0.07	0.10	0.18*	0.11	0.15	0.11	0.09	0.09
23.6%	5	1.	Temperature at jump	15.4	18.4	21.1	25.2	31.6	36.0	39.4	43.0	50.1
ethanol	)	2.	Depth of jump	0.15	0.07	0.13	0.15	0.12	0.18	0.09	0.08	0.11

*Note*.—There is some anomaly in the region of  $23^{\circ}$ C to  $27^{\circ}$ C in case of 21.8% ethanol solution, which shows two jumps close together, instead of the single one at  $25^{\circ}$ C in the case of the 20.0% and 23.6% solutions.



Fig. 2.—Chart showing plots of the temperatures at the various minima observed in the activation energy for the seven solutions in the range of 11% to 24% ethanol. The circles, triangles and crosses correspond respectively to jumps that are classified as large, medium or small, on the basis of comparison with the mean value of 0.11 for  $\Delta(E/R)/1000$ . It is seen that a smooth set of graphs can be drawn passing through these plotted points. The region between 11% and 16% is remarkable for the near constancy of the temperatures for most of the jumps.

Fig. 3.—It is reproduced directly below Fig. 2 from the previously published data of Qureshi and Khan, and the temperaures of the minima for two intermediate solutions viz. 6.9%and 8.2% e hanol (previously reported by Ahsanullah and Qurashi) are also plotted between these two Figs. 2 and 3. With the help of these intermediate points, the series of graphs in Figs. 2 and 3 are found to fit smoothly into each other. It is to be noted that the graphs of Figs. 2 and 3 generally bear out the earlier conjectures 4 regarding the definite dependence of the energy jumps on ethanol concentration, but in addition point to the presence of some significant structural changes associated with the branching out of two jumps from a single one. The appearance and growth of these subsidiary activation energy jumps is an intriguing phenomenon in itself, and it is hoped to make a finer study of this, with particular reference to the very dilute solutions below 5% ethanol.

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