THE ANOMALOUS BEHAVIOUR OF SOLUTIONS OF SIMPLE AROMATIC COM-POUNDS IN STRAIGHT-CHAIN HYDROCARBONS AND MINERAL OILS

Part I.—Viscosity Depression Measurements at Various Temperatures in the Binary Systems: Benzene-Heptane and Heptane-Cyclohexane

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In continuation of previous investigations on long-chain phenolic additives for oils, accurate measurements of viscosity depression have been made every 5 °C. from 15 °C. to 40°C. over the full range of concentrations in the binary system of benzene-heptane; for comparison, the heptane-cyclohexane system has been similarly measured. Viscosity depressions of the order of 12% of the ideally interpolated viscosity are observed in the benzene-heptane system, and the maximum relative viscosity depression $(\Delta \nu/\nu)$ appears to show an anomalous variation with temperature. The heptane-cyclohexane control gives only 4% depression and does not show the temperature variation anomaly.

A quantitative estimate of the excess free energy of mixing is made at about 180 cal./mole for benzeneheptane, and the phenomena are consistent with the existence of an appreciable interaction between benzene molecules, which might be of the order of 1/4 of that in most polar molecules. Further investigations on benzene and on related binary systems are in hand.

I. Introduction

In previous communications from this laboratory¹,²,³ dealing with long and short-chain phenolic compounds, it was shown that because the viscosity of these phenolic compounds is strongly dependent on both the length of the side chain and the number of active phenolic groups, the viscosity depression Δ_{\vee} produced by mixing them with a straight mineral oil (of the same viscosity) is better correlated with the actual viscosity rather than just the number of OH groups, and a relation of the form

$$\log (\Delta v) = A + 1.33 \log v = A + \log v^{1.33} (1)$$

was found to fit the results for both the $C_{15}H_{27}$ side chain and the C_3H_5 allyl side chain (Figure 5 in ref. 3). Two most striking observations made in the course of this generalization were (i) the existence of a very appreciable viscosity depression with both allylbenzene³ and dimethoxybhilawanol,² neither of which has any active OH groups, and (ii) the occurrence of an actual increase in viscosity near the 2-phase boundary for allylcatechol and mineral oil.³,⁴

The discovery of these phenomena has prompted a study of similar compounds without a side chain, viz. benzene, phenol, toluene, and cyclohexane, etc., leading to an analysis of the viscosity effects (at various temperatures) when mixed with straight hydrocarbons. The present communication describes the results obtained on the benzene-heptane system in the range of 15°C. to 40°C., together with comparative measurements on the heptane-cyclohexane system. Further measurements, on oil solutions of phenol and toluene, will be reported in later papers in this series.

2. Experimental Procedure

Ideally, for best sensitivity, the straight-chain hydrocarbons or oils chosen for mixing with the compounds under study should have the same viscosity and nearly the same molecular size as the compound itself, but in practice a compromise is often necessary. Thus, normal heptane (M= 100, $v_{25} = 0.570$ c.s.) was selected for mixing with $(M=78, v_{25}=0.686 \text{ c.s.})$ because it benzene gives a good balance between equality of molecular weight and equality of viscosity at 25°C. Also, there is not much difference between their volatilities, the boiling points being 98°C. and 80°C., respectively. In the case of heptane-cyclohexane system, the heptane was blended with 20% of kerosene oil so that the viscosities of the two component liquids of the system are equal at about 25°C.

The mixtures in concentration steps of 10% (with extra ones at 5% and 95%) were prepared at room temperature and shaken in a stoppered flask to prevent differential evaporation losses. The viscosity measurements were carried out according to standard procedures, using calibrated B.S.S. No. 0 viscometer (constant=0.000,734) suspended vertically with drying tubes attached in a cylinderical Gallenkamp thermostat, the temperature of which was controlled to within 0.1 °C. The flow-time measurements were first made below room temperature (26 °C.) and then above room temperature so as to minimize the possible effects of fractional evaporation from the test solutions, the whole series of measurements for any one concentration being completed in one working day. The flow times ranged from 10 to 20 minutes, measured to 0.2 sec., so that a reproducibility of $\pm 0.000,6$ centistoke i.e. $\pm 0.1\%$ was easily obtained with four or five readings at each temperature. This would correspond to a temperature uncertainty of about ± 0.08 °C.

3. Results with the Benzene-Heptane System from 15°C. to 40°C.

Table 1(a) shows the values of kinematic viscosity obtained for pure dry benzene and pure heptane (Merck) at the various temperatures, compared with the standard (Timmermans, 5 Int. Critical and Landolt-Boernstein⁶ Tables) values. The agreement is satisfactory, the root-mean-square difference being 0.002,5 c.s. for benzene and 0.001,8 c.s. for heptane, both of which are less than 0.5% of the actual viscosities.

The measurements for the full range of concentrations of benzene in heptane are given in Table 1(b) for the six temperatures from 15.4 °C. to 40 °C., together with the values of videal, calculated by linear interpolation between vbenzene and vheptane, and the viscosity depression $\Delta \nu$ obtained from

$$-\Delta v = v_{\text{expt}} - v \text{ ideal.}$$
(2)

It should be noted here that (i) the values of vexpt and videal are given to the fourth place to avoid cumulative errors in evaluating Δv , and (ii) because the difference between vbenzene and vheptane is about 17% on the average, the use of linear interpolation (in place of the Kendall logarithmic form) will produce a (consistent) discrepancy of about 0.5% i.e. 0.003 c.s. near the middle of the concentration range (cf. ref. 2 and 3). This is only slightly greater than the experimental

errors in v and very much less than the calculated values of Δ v.

The values of Δv are plotted for the six temperatures in Fig. 1(a), while the corresponding graphs for $\Delta v/videal = (1 - vexpt/videal)$ are shown in Figure 1(b). These graphs bear witness to the accuracy of about ± 0.001 centistoke estimated for the results, and indicate that the benzene heptane system shows a maximum viscosity depression of 10 to 14% at a concentration of 54% to 58% benzene by weight. This may be compared directly with the corresponding figures (12% and 10%) previously obtained for allylbenzene and dimethoxybhilawanol in mineral oil at 40°C., thus showing the consistent nature of the effect, in agreement with equation (1).

Finally, a graph is also plotted in the inset to the right-hand half of Fig. 1(b) showing the temperature variation of 10 $(\Delta \nu/\nu)_m$, which gives a measure of the change ΔG_m in the free energy on mixing (cf. discussion). This graph exhibits a more or less definite singularity in the region of 30° to 35°C., with some suggestion of another one below 15°C. However, it must be noted that the magnitudes of the deviations from a smoothly decreasing curve are only 3 to 5 times the experimental errors.

4. Results with Cyclohexane in a Heptane-Oil Blend

In an effort to throw further light on the nature of these phenomena, it was considered necessary first to make a comparative study of a simple cyclic saturated compound showing a very small degree of residual valence or polar effect. Cyclohexane was selected for this purpose, having M =84 and $v_{25} = 1.14$ c.s. For mixing with it, a blend of four parts of heptane with one part of kerosene oil was prepared, and its viscosity is

TABLE 1(a).—Comparison of Measured Viscosities (Centistokes) of Benzene and Heptane with Standard Data.

	Benzer	ne	<i>n</i> -Heptane			
Temperature (°C.)	Observed	Standard	Observed	Standard		
15.4	0.7846	0.784±1	0.6280	0.625 ± 3		
20.0	0.7367	0.740 ± 1	0.6006	0.600 ± 1		
25.0	0.6863	0.685 ± 3	0.5713	0.570 ± 2		
30.0	0.6424	0.649 ± 4	0.5422	0.542 ± 3		
35.0	0.6058	0.606 ± 3	0.5211			
40.0	0.568°	0.569 ± 5	0.4990	0.501 ± 1		
	Root-mean-square			Root-mean-square		

compared with that of the cyclohexane (Merck) at various temperatures in Table 2(a). The values for viscosity of the heptane blend were also determined at the end of the main experiment as a check on reproducibility, and are seen to be consistently higher than the first set by about

0.001C.s. Table 2(a) also gives the values of kinematic viscosity of cyclohexane as calculated from the standard values given in the compilation by Timmermans⁵ and in the Landolt-Boernstein Tables.⁶ Our measured values are seen to agree well with these.

TABLE I	(b)V	VISCOSITY	MEASUREMENTS ON	BENZENE-HEPTANH	E SYSTEM,	WITH	DEDUCED	DEPRESSIONS,
			Δ	v AND IO $\Delta v / v_{id}$.				

% Benzene	Vexpt (C.S.)	vid (c.s.)	Δν (c.s.)	$10\Delta \nu/ u_{ m id}$	% Benzene	Vexpt (C.S.)	vid (c.s.)	Δν (c.s.)	$10\Delta \nu/\nu_{id}$
Temperature=15,4°C.				Temperature=20.0°C.					
0.0	. 6289	.6289	.000	0.00	0.0	.6006	. 6006	.000	0.00
5.0	.6208	.6367	.016	0.25	5.0	.5933	.6074	.014	0.23
10.0	.6153	.6445	.029	0.45	10.0	.5881	.6142	.026	0.42
20.0	.6072	.6601	.053	0.80	20.0	.5790	.6278	.049	0.78
30.0	.6036	.6756	.072	1.07	30.0	.5772	.6414	.064	1.00
40.0	.6028	.6912	.088	1.27	40.0	.5757	.6549	.079	1.21
50.0	.6109	.7068	.096	1.36	50.0	.5816	.6686	.087	1.30
60.0	.6233	.7222	.099	1.37	60.0	.5923	.6822	.090	1.32
70.0	.6447	.7379	.093	1.26	70.0	.6109	.6959	.085	1.22
80.0	.6762	.7534	.077	1.02	80.0	.6388	.7095	.071	1.00
90.0	.7199	.7690	.049	0.64	90.0	.6792	.7231	.044	0.61
95.0	.7474	.7768	.029	0.37	95.0	.7034	.7299	.026	0.36
100.0	.7846	.7846	.000	0.00	100.0	.7367	.7367	.000	0.00
Temperature=25.0°C.					Tempe	erature=30.0)°C.		
0.0	.5713	.5713	.000	0.00	0.0	.5422	.5422	.000	0.00
5.0	.5654	.5771	.012	0.21	5.0	.5378	.5472	.009	0.16
10.0	.5602	.5828	.023	0.39	10.0	.5354	.5522	.017	0.31
20.0	.5514	.5943	.043	0.72	20.0	.5286	.5622	.033	0.59
30.0	.5502	.6058	.056	0.92	30.0	.5253	.5722	.047	0.82
40.0	.5485	.6173	.069	1.12	40.0	.5242	.5823	.058	1.00
50.0	.5529	.6288	.076	1.21	50.0	.5287	.5923	.064	1.08
60.0	.5630	.6403	.077	1.20	60.0	.5374	.6023	.065	1.08
70.0	.5794	.6518	.072	1.10	70.0	.5502	.6123	.062	1.01
80.0	.6087	.6633	.055	0.83	80.0	.5745	.6224	.048	0.77
90.0	.6424	.6748	.032	0.47	90.0	.6061	.6324	.026	0.41
95.0	.6608	.6806	.020	0.29	95.0	.6229	.6374	.015	0.24
100.0	.6863	.6863	.000	0.00	100.0	.6424	.6424	.000	0.00
	Tempe	rature=35.0°	°C,			Temp	erature=40.	0°C.	
0.0	5211	5211	.000	0.00	0.0	4990	4990	000	0.00
5.0	5163	5253	.009	0.17	5.0	4952	5024	007	0.14
10.0	5112	5296	.018	0.34	10.0	4900	.5059	.016	0.32
20.0	5045	5380	.034	0.63	20.0	4839	5128	029	0.57
30.0	.5021	5465	.044	0.81	30.0	.4788	.5197	.041	0.79
40.0	4997	.5550	.055	1.00	40.0	.4780	.5266	.049	0.93
50.0	.5026	.5634	.061	1.08	50.0	.4810	.5335	.052	0.98
60.0	.5111	.5720	.061	1.06	60.0	.4870	.5404	.053	0.98
70.0	.5231	.5804	.057	0.98	70.0	.4979	.5473	.049	0.90
80.0	.5456	.5889	.043	0.73	80.0	,5152	.5542	.039	0.71
90.0	.5721	.5973	,025	0.42	90.0	.5380	.5611	.023	0.41
95.0	.5867	.6016	.015	0.25	95.0	.5544	.5645	.010	0.18
100.0	.6058	.6058	.000	0.00	100.0	.5680	. 5680	.000	0.00

Note.—The fourth figures in the values of v_{expt} and v_{ijeal} are given merely to avoid cumulative errors in calculating Δv which is given only to three places.

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Temperature (°C.)	Heptane-oil ble	end	Cyclohexane		
	Initial	Final	Observed	Standard	
15.4	1.2527	1.2546	1.344	1.340±2	
20.0	I.I702	1.1700	1.245	1.250 ± 2	
25.0	1.093;	I.0944	1.147		
30.0	1.0249	1.0255	1.060	1.066±2	
40.0	40.0 0.9058 Average increase of 0.001,0 c.s.		0.915 Root-mean-s difference=0	quare 0.005 c.s.	

TABLE 2(a).—COMPARISON OF VISCOSITIES (IN CENTISTOKES) OF (I) HEPTANE-OIL BLEND,(II) CYCLOHEXANE AS OBSERVED, AND (III) CYCLOHEXANE FROM STANDARD DATA.

TABLE 2(b).—MEASURED VISCOSITIES FOR CYCLOHEXANE-HEPTANE (BLEND)	SYSTEM, WITH
DEDUCED DEPRESSIONS, Δv and $10(\Delta v/v_{id})$.	

Wt. % Cyc. hex.	V expt (c.s.)	vid. (c.s.)	Δv (c.s.)	$10\Delta u/ u$ id	Wt. % cyc. hex.	Vexpt (C.S.)	vid. (c.s.)	Δν (c.s.)	$10\Delta v/v$ id
	Temper	rature—15 d	°C				perature-20	0°C	
0.0	1 254	1 254	000	0.00	0.0	1 171	1 171	000	0.00
5.0	1 241	1 258	.000	0.14	5.0	1 163	1 175	012	0.10
10.0	1 237	1 263	026	0.21	10.0	1 159	1 178	019	0.16
20.0	1.231	1.272	.041	0.32	20.0	1,153	1,186	.033	0.28
30.0	1.231	1.281	.050	0.39	30.0	1,152	1,193	.041	0.34
40.0	1.230	1.290	.060	0.46	40.0	1.150	1.201	.051	0.42
50.0	1.233	1.299	.066	0.51	50.0	1.153	1.208	.055	0.46
60.0	1.239	1.308	.069	0.53	60.0	1.157	1.215	.058	0.48
70.0	1.255	1.317	.062	0.47	70.0	1.170	1.223	.053	0.43
80.0	1.277	1.326	.049	0.37	80.0	1.188	1.230	.042	0.34
90.0	1.304	1.335	.031	0.23	90.0	1.213	1.238	.025	0.20
95.0	1.323	1.340	.017	0.13	95.0	1.227	1.241	.014	0.11
100.0	1.344	1.344	.000	0.00	100.0	1.245	1.245	.000	0.00
	Temper	$ature = 25.0^{\circ}$	°C.			Ten	nperature=3	0.0^C.	
0.0	1.094	1.094	.000	0.00	0.0	1.025	1.025	.000	0.00
5.0	1.088	1.097	.009	0.08	5.0	1.018	1.027	.009	0.09
10.0	1.084	1.099	.015	0.14	10.0	1.014	1.029	.015	0.15
20.0	1.080	1.105	.025	0.23	20.0	1.009	1.032	.023	0.22
30.0	1.075	1.110	.035	0.32	30.0	1.005	1.036	.031	0.30
40.0	1.075	1.115	.040	0.36	40.0	1.004	1.039	.035	0.34
50.0	1.074	1.120	.046	0.41	50.0	1.003	1.043	.040	0.38
60.0	1.077	1.126	.049	0.44	60.0	1.005	1.047	.042	0.40
70.0	1.086	1.131	.045	0.40	70.0	1.012	1.050	.038	0.36
80.0	1.101	1.136	.035	0.31	80.0	1.023	1.054	.031	0.29
90.0	1.121	1.142	.021	0.18	90.0	1.039	1.057	.018	0.17
95.0	1.133	1.144	.011	0.10	95.0	1.049	1.059	.010	0.09
100.0	1.147	1.147	,000	0.00	100.0	1.061	1.061	.000	0.00
						Tempe	erature=40.0)°С.	
					0.0	0.906	0.906	.000	0.00
					5.0	0.901	0.906	.005	0.06
					10.0	0.898	0.907	.009	0.10
					20.0	0.892	0.908	.016	0,18
					30.0	0.888	0.909	.021	0.23
					40.0	0.884	0.909	.025	0.28
					50.0	0.882	0.910	.028	0.31
Note.	Measuremen	ts at 35°C. v	vere omitted	l because of	60.0	0.880	0.911	.031	0.34
Sec. Sec. A	the relatively	y small chang	ges with tem	perature in	70.0	0.885	0.912	.027	0.30
1	this region.				80.0	0.891	0.913	.022	0.24
					90.0	0.903	0.914	.011	0.12
					95.0	0.908	0.915	.007	0.08
					100.0	0,915	0.915	.000	0.00

The measurements on the mixtures over the full range of concentrations were carried out as for benzene-heptane, but omitting the readings at 35 °C. because of the smaller changes with

temperature in this case, and the results are shown in Table 2(b) together with the linearly interpolated values of ν_{ideal} and the values of viscosity depression deduced as before from



Fig. 1.-(a) Graphs for the measured viscosity depression $\Delta \nu$ (in centistokes) for the benzene-heptane system plotted against % benzene concentration at various temperatures from 15°C. to 40°C. (b) Corresponding graphs for 10 $\Delta \nu/\nu_{id}$, with the inset showing the anomalous temperature variation $10(\Delta \nu/\nu_{id})$ max.

 $-\Delta v = v \exp t - v \text{ ideal.}$ Fig. 2(a) shows plots of Δv against weight% cyclohexane for the five temperatures, and Fig. 2(b) below shows those for $10\Delta v/v$. These graphs show that $\Delta v/v$ at the minima is about 0.04, so that the deviation from ideal behaviour is only 1/3 of that in the case of benzene-heptane, which is in satisfactory agreement with the fact that the cyclohexane molecule, being fully saturated, exhibits a very small degree of residual interaction.

Also interesting is the plot of $IO(\Delta \nu / \nu)$ max against temperature in the inset to Fig. 2(b) which shows a smooth graph with a uniformly diminishing slope with increasing temperature, as would be expected in the absence of any anomalous interactions between molecules. This is to be contrasted with the corresponding graph for the benzene-heptane system (inset to Fig. I(b)).

5. Conclusions and Discussion

Thus, we may, by comparison with the cyclohexane-heptane system, conclude that benzene in heptane exhibits a significant anomalous behaviour, showing a viscosity depression with $(\Delta v/v)_{max}$ of the order of 0.12, which is comparable with that observed earlier in mixtures of allylbenzene and dimethoxybhilawanol with mineral oils²,³ of appropriate viscosity. In addition, the present measurements on the benzene-heptane system



Fig. 2.—(a) Graph showing the viscosity depression $\Delta \nu$ (in centistokes) measured for cyclohexane in heptaneoil⁺blend, plotted against weight % cyclohexane at various temperatures from 15°C. to 40°C. (b) Corresponding curves for $10\Delta\nu/\nu_{id}$, with the inset showing the normal character of the temperature variation for $10(\Delta\nu/\nu_{id})$ max.

have brought to light the existence of a further anomaly in the temperature variation of the maximum relative viscosity depression, $(\Delta v/v)_{max}$. As seen in the inset to Fig. 1(b), this quantity does not show the expected smooth drop with rising temperature, but instead presents the appearance of a rapid drop between two regions of near constancy. While a viscosity depression of 5% is noticeable in earlier reported data on hexane-benzene,7 the above-mentioned type of temperature variation of $(\Delta v/v)$ does not appear to have been observed previously and its study should therefore be of some importance.

It is interesting to examine the origin of the above behaviour, because the large viscosity depression points to a significant polar interaction of the benzene nucleus in solutions of straightchain oils, in agreement with equation (1). Presumably, the effect is to be connected with the residual intermolecular forces emanating from the resonating π -electrons of the benzene ring. We can make some estimate of the change in free energy ΔG_m on mixing, corresponding to the values of $(\Delta v/v)$ observed in Fig. 1(b), by utilizing the following approximate theoretical⁸ equation:

$$\eta_{\text{expt.}/\eta \text{ideal}} \simeq \exp[-\Delta G_m/2.45 \text{RT}]$$
 (3)

in which the factor 2.45 is found empirically to give good agreement with experimental data on several systems.⁹ This equation leads to

$$\Delta G_{\rm m} = 2.45 \text{ RT } \ln (\eta i / \eta_{\ell})$$

2.45 RT ($\Delta \eta / \eta$) $\simeq 2.45 \text{ RT } (\Delta \nu / \nu)$ (4)

because $\frac{\Delta v}{v} \simeq \frac{\Delta \eta}{\eta} << 1$. This shows that over

a small range of temperatures, ΔG_m is proportional to $+ (\Delta \nu / \nu)$; for T $\simeq 300 \,^{\circ}$ K. (room temperature), the constant of proportionality is nearly 1,500 cal./mole. It follows that for the benzene-heptane interaction, at the greatest viscosity depression, Gm is nearly 180 cal./mole, which is of the order of 1/4 to 1/2 the figures for several polar molecules.9 This suggests that viscosity depression is probably to be explained in terms of the greater strength of the benzene-benzene interactions as against benzeneheptane. The shape of the curves for Δv against concentration of benzene is very similar to that observed for allylbenzene3 and allylphenol,3 and it appears likely that a theoretical formulation can be given along the lines of that previously used¹⁰ to connect the hydrogen-bond concentration (determined from infrared measurements)

with the viscosity depressions observed for allylphenol in oil. It is hoped to publish a detailed account after analyzing measurements with toluene, phenol, etc.

As regards the anomaly in the temperature variation of the relative viscosity depression (inset to Fig. 1(b), since $(\Delta \nu / \nu)$ is proportional to Δ G_m by equation (4), it follows that this excess free energy of mixing apparently varies in a periodic manner with temperature, showing successive regions of constant value and a rapid drop from one to the next. This is rather similar to the segments and steps already observed in the activation energy of several pure associated liquids e.g. glycerol, ethylene glycol, water,¹¹ and the present experiments thus suggest that it would be worthwhile to examine various other binary mixtures as well as pure benzene for the possible existence of such an effect.

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